Many things are made in the shape of a cuboid, such as drink cartons and cereal boxes. This activity is about finding the volumes of cuboids.

## Information sheet

The volume of an object is the amount of space it fills.

Large volumes are measured in cubic metres $\left(\mathrm{m}^{3}\right)$.
Smaller volumes are measured in cubic centimetres $\left(\mathrm{cm}^{3}\right)$ or cubic millimetres $\left(\mathrm{mm}^{3}\right)$.


In this cuboid there are 3 layers of cubes. There are 2 rows of 4 cubes in each layer.

The total number of cubes $=4 \times 2 \times 3$
The volume of the cuboid $=4 \times 2 \times 3=\mathbf{2 4} \mathbf{c m}^{\mathbf{3}}$


For any cuboid:
Volume $=$ length $\times$ width $\times$ height
or Volume $=$ area of cross-section $\times$ length


The volume of liquids is usually measured in litres or millilitres.

$$
\begin{aligned}
& 1 \text { litre }=1000 \mathrm{ml} \text { and } 1 \mathrm{ml}=1 \mathrm{~cm}^{3} \\
& 1 \text { litre }=1000 \mathrm{~cm}^{3} \text { and } 1 \mathrm{~m}^{3}=1000 \text { litres }
\end{aligned}
$$

## Fish tank example

Volume of fish tank $=120 \times 50 \times 60$
$=120 \times 3000$
$=360000 \mathrm{~cm}^{3}$
Volume of fish tank = $\mathbf{3 6 0}$ litres.
(Check the calculation on your calculator.)


Note the volume of a container for liquids is often called its capacity.
It is important that all the dimensions of the cuboid are in the same units.

## Concrete block example

Find the volume of a concrete block that is 2.5 metres long, 12 centimetres wide and 10 centimetres high.


Two of the dimensions, the width and height, are in centimetres.
Converting the length to centimetres: $2.5 \mathrm{~m}=2.5 \times 100=250 \mathrm{~cm}$


Volume of concrete block $=250 \times 12 \times 10$

$$
=2500 \times 12
$$

Volume of concrete block $=\mathbf{3 0 0 0 0} \mathrm{cm}^{3}$
(Check the calculation on your calculator.)

## Sand pit example

A sand pit is 2 metres long and 1.5 metres wide.
How much sand will it take to fill the sandpit to a depth of 20 centimetres?
In this case, two of the dimensions, the length and width, are in metres.
Converting the height to metres: $20 \mathrm{~cm}=20 \div 100=0.2 \mathrm{~m}$

Volume of sand needed
$=2 \times 1.5 \times 0.2$
$=3 \times 0.2$
Volume of sand needed $=0.6 \mathrm{~m}^{3}$
(Check the calculation on your calculator.)


## Try these

Work out your answer for each question in the box.

1 A heating engineer needs to work out the volume of this room.
What is its volume?


2 All the edges of this dice are 10 mm long.
What is its volume?


3 A brick is 20 cm long, 12 cm wide and 10 cm high.
What is its volume?


4 A storage box is 1.5 m long, 1.2 m wide and 1 m high.
Find its volume.


5 The picture shows a block of cheese.
What is its volume?


6 The picture shows the dimensions of a fish tank. Find its volume (capacity) in cubic metres.


7 The diagram shows the dimensions of a waste disposal container. What is its volume?


8 A stock cube is 20 mm long, 20 mm wide and 20 mm high. Calculate its volume.


9 A carton of orange juice measures 9 cm by 6 cm by 19.5 cm . Show that its volume is just over 1 litre.


10 A rectangular swimming pool is 25 m long and 10 m wide.
How many litres of water do you need to fill it to a depth of 2 m ?


11 Ice-cream mixture is poured into a container to make a block of ice-cream 20 cm long, 8 cm wide and 5 cm high.
a Find the volume of the block.

b How many blocks can you make with 4 litres of ice-cream mixture?
$\square$

12 A builder plans a tarmac drive for a new house.
The drive is in the shape of a rectangle 12 metres long and 3 metres wide.
The tarmac needs to be 20 cm thick.
What volume of tarmac does the builder need?
$\square$

13 A rectangular paddling pool is 2.5 m long and 2 m wide.
How many litres of water do you need to fill it to a depth of 40 cm ?
$\square$
14 What volume of concrete is needed for a path which is 80 metres long, 1.5 metres wide and 150 mm deep?
$\square$

## At the end of the activity

- A manufacturer needs to know the volume of a box (cuboid). Explain how to find this.
- What units can volume be measured in?
- Suggest dimensions you could use to make a carton with a volume of 1 litre ( $1000 \mathrm{~cm}^{3}$ ).

